The roles of migratory and resident birds in local avian influenza infection dynamics

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Abstract

1. Migratory birds are an increasing focus of interest when it comes to infection dynamics and the spread of avian influenza viruses (AIV). However, we lack detailed understanding of migratory birds’ contribution to local AIV prevalence levels and their downstream socio-economic costs and threats.

2. To explain the potential differential roles of migratory and resident birds in local AIV infection dynamics, we used a susceptible-infectious-recovered (SIR) model. We investigated five (mutually non-exclusive) mechanisms potentially driving observed prevalence patterns: 1) a pronounced birth pulse (e.g. the synchronised annual influx of immunologically naïve individuals), 2) short-term immunity, 3) increase of susceptible migrants, 4) differential susceptibility to infection (i.e. transmission rate) for migrants and residents, and 5) replacement of migrants during peak migration.

3. SIR models describing all possible combinations of the five mechanisms were fitted to individual AIV infection data from a detailed longitudinal surveillance study in the partially migratory mallard duck (Anas platyrhynchos). During autumn and winter, the local resident mallard community also held migratory mallards that exhibited distinct AIV infection dynamics.

4. Replacement of migratory birds during peak migration in autumn was found to be the most important mechanism driving the variation in local AIV infection patterns. This suggests that a constant influx of migratory birds, likely immunological naïve to locally circulating AIV strains, is required to predict the observed temporal prevalence patterns and the distinct differences in prevalence between residents and migrants.

Synthesis and applications. Our analysis reveals a key mechanism that could explain the amplifying role of migratory birds in local avian influenza virus infection dynamics; the
constant flow and replacement of migratory birds during peak migration. Aside from monitoring efforts, in order to achieve adequate disease management and control in wildlife - with knock-on effects for livestock and humans, - we conclude that it is crucial, in future surveillance studies, to record host demographical parameters such as population density, timing of birth and turnover of migrants.

Introduction

Highly pathogenic avian influenza (e.g. H5N1, H5N8) is a prime example of an emerging infectious disease with rapid rise in incidences in poultry, and potentially in humans and wild birds (Alexander 2007). When it comes to the spread and local amplification of avian influenza viruses (AIV), herewith threatening global economies and public health, migratory birds are increasingly thought to play a central role (Lycett et al. 2016). Several characteristics of migratory species make them seemingly perfect vectors for a variety of pathogens (Altizer, Bartel & Han 2011). During their migratory journey migrants may encounter a broad range of parasite species and strains, thereby increasing the likelihood of transmitting novel parasites to resident communities they encounter en-route (Waldenström et al. 2002). Moreover, the physiological challenges migrants face during their migration, leading to potential trade-offs with their immune function, may increase their susceptibility to infection (Buehler et al. 2008). Finally, many migrants aggregate in large numbers at so-called stop-over sites leading to further enhancement of pathogen transmission (Krauss et al. 2010; Fritzsche McKay & Hoye 2016). However, despite the pervasive support for the role of migrants in pathogen dispersal (e.g. Fourment, Darling & Holmes 2017), conceptual support of clearly documented and quantified examples of their role in infection dynamics are surprisingly rare (Altizer,
Bartel & Han 2011). This significantly constrains our ability to design strategies to recognise
and mitigate potential disease threats coming from wildlife populations, which in turn could
minimize the risk of spill-over to domestic animals and humans.

In this study, we built on a unique dataset from a detailed study on mallard ducks (Anas
platyrhynchos); van Dijk et al., (2014) described AIV infection dynamics at a small spatial
scale, a single duck decoy, over a full annual cycle. During part of the year (i.e. autumn and
winter), the local mallard community consisted of resident and migratory birds and by
characterizing the majority of individuals as either migratory or resident, van Dijk et al. (2014)
showed that the major peak of AIV infection in autumn coincided with the arrival of
susceptible migratory mallards. Here, we use a Susceptible-Infectious-Recovered (SIR)
modelling framework, aiming to explore multiple mechanisms that are suggested to drive
local AIV infection dynamics in wild birds, quantify their relative importance, and identify the
differential role of migrants and residents within the population. We start with a very basic
demographic and epidemiological model, gradually increasing the complexity by adding and
combining the following five, non-mutually exclusive, mechanisms:

1 – Birth pulse: The synchronised hatching of chicks can be a major factor influencing
seasonal changes to the density of susceptible individuals. The vast majority of animal
populations show marked seasonal variation in the timing of birth, resulting in a pulsed influx
of immunologically naïve juveniles (Hosseini, Dhondt & Dobson 2004; Begon et al. 2009).
Such seasonal birth pulses have been shown to both precede annual peaks in infection
prevalence in wildlife (Hinshaw et al. 1985; Peel et al. 2014; Avril et al. 2016), and be
fundamental to producing these dynamics in empirically validated models (Hosseini, Dhondt
Short-term immunity: The vast majority of theoretical AIV infection studies assume long-term or even permanent immunity (e.g. Galsworthy et al. 2011; Nickbakhsh et al. 2014). In fact, the immune response to AIV within the host appears to be sufficient to attenuate the duration and the intensity of subsequent infections (Fereidouni et al. 2010; Jourdain et al. 2010). However, the relatively weak antibody response may be short-term and antibodies might be detectable for a few months only (Kida, Yanagawa & Matsuoka 1980; Hoye et al. 2011; Samuel et al. 2015).

Increase of susceptible migrants: A key feature that put migrants into the spotlight of infectious disease dynamics is the fact that they visit disparate locations throughout their annual cycle (Altizer, Bartel & Han 2011). In combination with the rather strain-specific immune response to AIV infections (Jourdain et al. 2010), migrants may thus be generally more susceptible to local AIV strains once they arrive at a new location (Verhagen et al. 2014).

Differential susceptibility: The physiological challenges associated with migratory journeys may result in a trade-off with immune functioning, leading to a reduced immunocompetence in migrants compared to residents (Altizer, Bartel & Han 2011). These differences in immune status may translate into a higher likelihood of migrants becoming infected with AIV after contact with an infectious individual.

Replacement of migrants: In the context of infectious disease dynamics, like with AIV, a yet understudied part of migration is the diversity in migratory strategy. At one extreme all individuals of a population may have an identical spatial-temporal pattern in their migration (e.g. Orell et al. 2007; Stanley et al. 2012), while at the other end of the spectrum, individuals migrate within a broad time window and may not necessarily follow the same
route. These differences in migration timing and arrival can have profound effects on the
local composition, density and turnover of individuals at breeding, wintering and staging
sites, and therewith on the local host-pathogen dynamics (Møller & Szep 2011; Bauer,
Lisovski & Hahn 2016).

Materials and Methods

Study Species

Mallards are one of the most common and numerous waterfowl species around the world,
with an estimated population size of 19 million individuals (Delany & Scott 2006). The species
is also considered to be the major AIV reservoir in the wild (Webster et al. 1992). Mallards
are partially migratory, meaning that the population consists of both migratory and resident
birds. Birds breeding in western Europe (e.g. the Netherlands) are mainly sedentary, and
northern breeding birds (e.g. Scandinavia, the Baltic, north-west Russia) migrate in autumn to
overwinter between Denmark, northern France and Britain (Scott & Rose 1996).

Study Site and Sampling

Detailed description of the sampling diagnostic methods can be found in van Dijk et al.
(2014). In short, mallards were caught using swim-in traps of a duck decoy (Payne-Gallwey
1886) located near Oud Alblas (4°42’26”E, 51°52’38”N), the Netherlands. Sampling took
place from March 2010 until February 2011. On average, the duck decoy was visited six times
per month, capturing approximately 15 individuals per visit, resulting in a total of 1109
samples being collected. For detection of current AIV infection, both cloacal and
oropharyngeal samples were taken and analysed. To determine the origin of the individuals,
thus distinguishing between migrants and residents, stable hydrogen isotope ($\delta^2$H) ratios
were measured within freshly moulted feather collected from the individuals caught
between August and December. The origin of 319 out of 458 individuals could be classified (van Dijk, Meissner & Klaassen 2014).

Modelling

All five potential mechanisms (“modifications” hereafter) had an identical underlying “basic” model (Figure 1), describing mallard demography – birth, death, migration – at the study site and the basic AIV infection dynamics.

Basic model structure

The AIV infection dynamics were modelled using a $SIR$ model with the components Susceptible ($S$), Infectious ($I$) and Recovered ($R$) (Figure 1). Infections are generally thought to be density dependent (McCallum, Barlow & Hone 2001), and modelled with a transmission term $\beta$, describing the rate at which susceptible birds ($S$) become infected through direct or indirect contact with infectious individuals ($I$). For AIV, indirect transmission is considered to be of crucial importance and follow a faecal-oral route via water (Webster et al. 1992). In addition to the $\beta$ term for transmission, we allowed for background transmission ($\eta$) to account for virus persistence in water (e.g. Stallknecht et al. 1990), because environmental transmission can potentially occur after infectious individuals have left the site. However, background transmission was set to a low value given that Nazir et al. (2010) found persistence of AIV to range between days to a couple of weeks depending on temperature. Most importantly background transmission allows occasional re-introduction of the virus in the absence of infectious birds and is a crucial mechanism enabling the persistence of pathogens, particularly within small wildlife communities that are below the critical community size where epidemics cannot be sustained by direct transmission only (Breban et al. 2009). Birds that recovered from AIV infection at rate $\gamma$, were moved from the infectious compartment ($I$) to the recovered compartment ($R$). Loss of immunity occurred at rate $\sigma$,
transferring individuals from the recovered \((R)\) to the susceptible \((S)\) compartment. Arriving
migrants were allocated across the susceptible \((S)\), infectious \((I)\) and recovered \((R)\)
compartments in the same proportions as the resident population.

The demography was modelled as an integral part of the SIR model, with separate differential
equations describing the migrant and resident population. The basic model assumed a
resident population of 700 adult individuals, reflecting the approximate number of residents
observed at the study site (van Dijk et al. 2014). Birth rate \((B(t))\) was modelled for residents
only and followed a normal distribution, defined by mean day of birth \((B_{\text{mean}})\) and its standard
deviation \((B_{sd})\), which was multiplied by the number of breeding pairs \((0.5 \cdot N_{\text{pop}}, \text{i.e. half the}
resident population size)\) and a fixed number of hatchlings per pair \((N_{\text{hatch}})\) to derive a daily
number of hatchlings that enter the population. All individuals (i.e. residents and migrants)
experienced natural mortality at rate \(m\). The arrival of migrants at rate \(M(t)\) was also
modelled following a normal distribution defined by mean arrival date \((A_{\text{mean}})\) and its standard
deviation \((A_{sd})\), which was multiplied by the resident population size \((N_{\text{pop}})\) and the ratio of
migrants to residents \((P_{\text{mig}})\). Departure of migrants was modelled by setting the migratory
population to 0 at day 92 (1\(^{\text{st}}\) of April), when migrants were expected to have left the area for
spring migration (Cramps & Simmons 1977).

These assumptions formed the basic model that consisted of six ordinary differential
equations:

\[
\frac{dS(t)}{dt} = -\beta(I_M + I_R)S_R + \sigma R_R - \eta S_R - mS_R + B(t) \left( \frac{1}{2} \cdot N_{\text{pop}} \right) N_{\text{hatch}} \quad \text{eq. 1}
\]

\[
\frac{dI(t)}{dt} = \beta(I_M + I_R)S_R - \gamma I_R + \eta S_R - mI_R \quad \text{eq. 2}
\]
\[
\frac{dR_R(t)}{dt} = \gamma I_R - \sigma R_R - mR_R \\
\text{eq. 3}
\]

\[
\frac{dS_M(t)}{dt} = -\beta (I_M + I_R)S_M + \sigma R_M - \eta S_M - mS_M + M(t)\left(\frac{S_R}{S_R + I_R + R_R}\right) N_{pop}Pr_m \\
\text{eq. 4}
\]

\[
\frac{dI_M(t)}{dt} = \beta (I_M + I_R)S_M - \gamma I_M + \eta S_M - mI_M + M(t)\left(\frac{I_R}{S_R + I_R + R_R}\right) N_{pop}Pr_m \\
\text{eq. 5}
\]

\[
\frac{dR_M(t)}{dt} = \gamma I_M - \sigma R_M - mR_M + M(t)\left(\frac{R_R}{S_R + I_R + R_R}\right) N_{pop}Pr_m \\
\text{eq. 6}
\]

192  
\textit{Migrant population:}

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\[
\frac{dS_M(t)}{dt} = -\beta (I_M + I_R)S_M + \sigma R_M - \eta S_M - mS_M + M(t)\left(\frac{S_R}{S_R + I_R + R_R}\right) N_{pop}Pr_m
\]

194  
\[
\frac{dI_M(t)}{dt} = \beta (I_M + I_R)S_M - \gamma I_M + \eta S_M - mI_M + M(t)\left(\frac{I_R}{S_R + I_R + R_R}\right) N_{pop}Pr_m
\]

195  
\[
\frac{dR_M(t)}{dt} = \gamma I_M - \sigma R_M - mR_M + M(t)\left(\frac{R_R}{S_R + I_R + R_R}\right) N_{pop}Pr_m
\]

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\textbf{Model modifications}

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For the 1\textsuperscript{st} modification \textit{birth pulse} we divided the resident population into adults (>10 months old) and juveniles (<10 months old), with 10 months being the period between hatching and sexual maturity in juveniles. Separation in age class allowed for differential mortality rates. At the end of the annual cycle (defined at day 92, April 1\textsuperscript{st}) all juveniles were transferred into the pool of adults. The 2\textsuperscript{nd} modification, \textit{short-term immunity}, did not require a structural change of the basic model. In the 3\textsuperscript{rd} modification, \textit{increase of susceptible migrants}, relatively more migrants (\(b\)) enter into the susceptible (\(S\)) compartment instead of being distributed across the three compartments according to the proportions of the resident population. In the 4\textsuperscript{th} modification, \textit{differential susceptibility}, we allowed for separate transmission rates for residents and migrants (\(\beta_R\) and \(\beta_M\), respectively). To model the 5\textsuperscript{th} modification, \textit{replacement of migrants}, a function describing this replacement was added \(R(t)\), which was modelled using a symmetric double logistic function with parameters mean, amplitude, slope and kurtosis (i.e. \(R_{mean}, R_{amp}, R_{slope}, R_{kurt}\) respectively). All model equations can be found in supplementary material S1.
Only few model parameters could be fixed at a value derived from literature or personal observations (Table 1). For most parameters, we lack data since these are often difficult or even impossible to measure. For ‘non-fixed’ parameters we defined a likely range (Table 1) over which they were allowed to vary during model simulations. Simulations were conducted with 32 different model scenarios, where each scenario consisted of a combination of the basic model and one or more of the five model modifications.

In the basic model, birth was modelled using a fixed number of 0.63 hatchlings per pair ($N_{\text{hatch}}$). This value ensured a stable population size over time given a natural daily mortality rate ($m$) of $8.63 \times 10^{-5}$, which was based on a life expectancy of 2.27 years for mallards (Schekkerman & Slaterus 2008). AIV transmission rates ($\beta$) in wildlife populations are largely unknown, therefore we chose a broad range for $\beta$, making sure that the basic reproduction number of the virus ($R_0$) ranges from 0.8 to 8.0. The background infection rate ($\eta$) was set to a fixed value of $\eta = 10^{-5}$, which gives a probability of 1% for a single mallard to become infected in a mean lifetime of 828 days (Galsworthy et al. 2011). The mean recovery rate ($\gamma$) and the immune loss rate ($\sigma$) can vary between host-species, their immunological history and between AIV strains (Costa et al. 2010; Fereidouni et al. 2010; Jourdain et al. 2010; Curran 2012). A mild strain may cause longer periods of virus excretion ($\gamma \approx 1/12$: Kida, Yanagawa & Matsuoka 1980; Costa et al. 2010; Jourdain et al. 2010), whereas a more severe strain may have a short generation time of approximately three days ($\gamma \approx 1/3$: Ng & Higgins 1986; van der Goot et al. 2008; Latorre-Margalef et al. 2009). The immune rate ($\sigma$) was set to a range resulting in a mean loss of immunity within 75 to 730 days. Mean autumn migration ($A_{\text{mean}}$) was set from August 27th to November 30th, depicting the period that migratory mallards may...
arrive at the wintering grounds in Western Europe. This period reflects the observed bird
migration window (Fransson & Petersson 2001; Bakken, Runde & Tjørve 2003).

For the 1st modification birth pulse, a larger number of hatchlings was chosen. Mallards are
known to produce large clutches with an average clutch size of 9 to 13 eggs (Cramp &
Simmons 1977), that potentially result in 4 instead of 0.63 hatchlings per pair \(N_{\text{pulse}}\) that
enter the resident population (Figure 1). Mortality rates for juveniles \(m_{\text{juv}}\) were estimated
prior to each simulation to ensure a stable population size \(N = 700\), taking the \(B_{\text{mean}}, B_{\text{sd}},\)
and \(m\) into account. The parameter boundaries describing the replacement of migrants \(R(t)\)
in the 5th modification replacement of migrants was defined to allow the replacement of
individuals at the start of the migratory period (August 27th) until mid-October, depicting the
peak of migration. Migrants with a current AIV infection were not subject to replacement,
since this would not change the number of infected individuals and the infection dynamic.
Although in reality, infected individuals might also be subjected to replacement. Empirical
studies in mallards and other waterfowl have shown that AIV infection may hamper
migration and movements (van Gils et al. 2007; van Dijk et al. 2015; Hoye et al. 2016),
suggesting that infected individuals may remain stationary during the course of an infection.

Simulation and model fit

To allow demographic and infection patterns to stabilize, all models were run over ten annual
cycles, where the last cycle was used for comparison with the empirical patterns observed in
the field. All possible model scenarios \(n = 32\) were written in C++ and compiled, as well as
integrated using the ‘ode’ method in R Package deSolve (Soetaert, Petzoldt & Setzer 2010).
To estimate parameter values, their relative importance and uncertainties, we used a Markov
Chain Monte Carlo (MCMC) simulation with a delayed adaptive Metropolis algorithm (Haario
et al. 2006), implemented in the function MCMCmod from R Package FME (Soetaert &
Petzoldt 2010). This MCMC algorithm uses a multivariate proposal distribution that is automatically adapted to allow for posterior corrections between parameters and identifies the direction of principal change along the ridges in the posterior landscape. The acceptance rate is improved by the delayed rejection part of the algorithm where, instead of immediately advancing the chain following rejection of a parameter set, a second proposal is made that depends on both the current position of the chain and the rejected parameter set. Ultimately, the DRAM algorithm produces posterior distributions of the parameters by minimizing the so-called ‘model costs’ defined as the negative sum of the log-binomial densities (binomial response of the number of infected and non-infected individuals).

For all possible model scenarios, we simulated 25 independent MCMC chains using 10,000 iterations with an update of the covariance matrix after every 50th iterations and one delayed rejection step. Initial parameters were chosen randomly from the parameter ranges for each MCMC chain. The possible parameter space for all non-fixed parameters is shown in Table 1. The last 2,500 iterations were used to describe the posterior distribution of each of the non-fixed parameters as well as to calculate the confidence interval of the model predication and the goodness of fit used to compare model scenarios based on Watanabe-Akaike information criterion (WAIC), a pointwise out-of-sample prediction accuracy (Watanabe 2010; Gelman et al. 2013). Within the DRAM optimization routine, observations for residents and migrants were compared separately with the respective model output (i.e. number of infected and non-infected individuals in residents and migrants). Sampling results of individuals with unknown migration status were also included in the model and compared with the pooled predicted prevalence in both residents and migrants. Thus, the best fitting model is based on the sum of three (i.e. resident, migrant, unknown status) separate ‘model costs’ (or the sum
of three log-binomial density distributions). We used median WAIC value for each model scenario to rank their potential in predicting the observed AIV infection dynamic. We investigated potential collinearity of model parameters for each of the scenarios by calculating the correlation matrix of the parameters across the final 2,500 iterations.

Results

Model scenarios

The basic model in combination with the five different model modifications led to 32 possible scenarios (Figure 2). The median WAIC values of the model fit for these 32 scenarios ranged from 135.5 to 324.6, with lower values indicating better model fits and a higher potential to predict the observed AIV infection dynamic. Although their annual AIV infection dynamics appeared slightly different, the best fitting three scenarios (rank 1 to 3) were within a small WAIC range of 4.8, and could be considered similarly good (Figure 2). In fact, the first 8 scenarios differed in their ability to predict the observed infection dynamic from the remaining scenarios with median WAIC values from 135.46 to 156.17 compared to > 172.3 in the ranks from 9 to 32. These 16 best ranked scenarios all included the 5th modification, the replacement of migrants. In addition to the 5th modification, modification 4 was found to increase the fit in the 8 best-ranked scenarios (Figure 2). This modification also contributed the 8 scenarios missing the 5th most important modification (rank 17 to 24).

The replacement of migrant modification was the best modification in explaining the observed WAIV prevalence pattern in isolation with the basic model (rank-12, Figure 2 and Figure 3). However, in isolation, the 4th modification resulted in a relatively poor fit (rank 22, Figure 3). No eminent pattern was found in the distribution of the other three modifications across the 32 scenarios ranked by their WAIC value (Figure 2).
Parameter estimates

Looking at the best parameter combinations across all 32 scenarios (Figure 2), once the transmission rates were modelled separately for migrants and residents (thus including the 4th differential susceptibility modification), $\beta_M$ was estimated higher than $\beta_R$ except for rank 6 that was the only scenarios where $\beta_M$ was chosen within the boundaries of $\beta_R$. The recovery rates ($\gamma$) were almost always at the lower end of the pre-defined parameter range: AIV infected individuals recovered after an average of approximately 12 days. The immune rates ($\sigma$) were highly variable across the different scenarios and thus unrelated to the goodness of fit (WAIC value) of the models. However, in all scenarios that included short-term immunity, the rate ($\sigma_s$) was higher than it would have been in the absence of the 2nd short-term immunity modification. This was notably true for scenarios missing the 4th and the 5th modification when short-term immunity was the mechanism that could elevate the prevalence levels during the late summer and autumn period. In almost all scenarios, the ratio of migrants to residents ($Pr_{mig}$) was highly skewed towards migrants: 3-4 times the resident population.

In general, across the first 16 scenarios that included the 5th replacement of migrants modification, the arrival peak of migrants ($A_{mean}$) occurred relatively early (low $A_{mean}$) with respect to the pre-set window (early August). In contrast, without this modification, peak arrival dates occurred in mid-October. The shape of the arrival curve ($A_{sd}$) was consistently in the lower half of the pre-set parameter range and was particularly low, i.e. reflecting a quick and synchronised arrival, in the best fitting scenarios. Not much variation was found in the timing of replacement ($R_{mean}$), i.e. the start was always at the upper boundary and therefore as early as possible. The amplitude of the replacement curve ($R_{amp}$) varied, but was consistent within the upper half of the parameter range (0.35-0.6).
Parameter correlation

We used the posterior distributions of each parameter from the last 2,500 MCMC iterations to illustrate the potential correlation between parameters. In the best ranked model scenario (rank 1) that included the 2nd short-term immunity, the 4th differential susceptibility and the 5th replacement of migrants modification, many parameters showed high correlation (indicating parameter identification problem), e.g. the recovery rate (γ) was positively correlated with the transmission rate of the resident population (β_R). Whereas the immune rate (σ) was negatively correlated with the transmission rate of the migrant population (β_M). This means that all four parameters could contribute to higher prevalence levels during the major peak. Additionally, the shape of the replacement of migrants distribution (R_{sd}) was found to be correlated with the transmission rates of residents (γ) and the immune rate.

However, correlations between parameters different immensely between the scenarios (supplementary material S2).

Discussion

Mathematical modelling has great potential to probe the complex dynamics of infectious diseases and identify the mechanisms of transmission. Therewith, it may also indicate approaches for prevention and control that may help shape national and international public health policy (Heesterbeek et al. 2015). In this study, we used a mathematical modelling approach to evaluate several mechanisms that have been suggested to drive local AIV dynamics in wild bird populations. To evaluate these mechanisms, we fitted the predicted infection dynamics to a unique sampling dataset of a year-round, small-scale AIV surveillance study in the key European AIV host species, the mallard (van Dijk et al. 2014). We found that
one particular mechanism, the local replacement of migrants during the peak migration, contributed most significantly towards better model predictions. There is a general perception that animal migration plays a central role in wildlife disease dynamics by enhancing the global spread of pathogens (Altizer, Bartel & Han 2011). Notably with respect to AIV there are a number of high-profile studies stressing this case (Verhagen, Herfst & Fouchier 2015; Hill et al. 2016; Lycett et al. 2016). In addition, we show that migrants may importantly facilitate local AIV infection dynamics. Our models provide strong indications that the role of migrants in infection dynamics is not simply determined by the presence of migrants, but critically relies on how migration takes place over time. Migratory birds within a population may migrate highly synchronised and visit stop-over sites all at once, or they may differ in their timing leading to several waves of migrants and extended periods during which migrants arrive at and depart from stop-over sites (Bauer, Lisovski & Hahn 2016). In most species, including the mallard (Fransson & Petersson 2001; Bakken, Runde & Tjorve 2003), the migratory season protracts over several weeks up to a few months. This is likely to lead to the mechanisms behind migratory replacement used as a modification in our model: arriving migrants stay in the area for a limited period of time after which they move on and are replaced by newly arriving individuals. As a consequence, individuals that have acquired some degree of protection against re-infection by means of AIV specific antibodies (either due to AIV exposure prior to arrival or at the study site itself), are replaced by potentially susceptible individuals that may perpetuate or even invigorate local transmission dynamics. Besides the strong effect of the replacement of migrants, the models with better predicting power also included the modification differential susceptibility with higher transmission rates in migrants compared to residents. This is in line with the observed data showing that the
major AIV prevalence peak coincided with the arrival of migrants (van Dijk et al. 2014). There are several non-mutually exclusive mechanisms that may explain why the better predicting models had an increased susceptibility in individual migrants. Empirical studies have shown that the physiological challenges accompanied with migration, including a potential trade-off with the immune system, can reduce their immunocompetence and render migrants more susceptible (Buehler et al. 2008). It has also been suggested that migrants are generally more susceptible, since their immune system is less specialised but adapted to cope with the exposure of different and disparate environments and their pathogens (Waldenström et al. 2002).

Combining the findings from the model and the empirical study, we can conclude that migrants may not exclusively affect the AIV infection dynamics of resident populations through their often suggested role in the introduction of new virus strains (e.g. Verhagen, Herfst & Fouchier 2015; Lycett et al. 2016) and the general increase in host-densities (Gaidet et al. 2012, Hill et al. 2012), but may have an additional role in the amplification of the virus (Yin et al. 2017). Since migration is a large-scale multi-species phenomenon, this might more generally be the case and it questions the hypothesis that migrants only have a role in dispersing and introducing AIVs and thereby affecting resident populations.

Most northern hemisphere AIV surveillance studies in wild bird populations show similar patterns of pronounced late summer - early autumn infection peaks (e.g. Munster et al. 2007; Hénaux et al. 2013; Lisovski, Hoye & Klaassen 2017). Clearly, our model scenarios are ranked by their ability to capture this pronounced feature within the entire annual infection dynamic. While allowing for differential susceptibility to infection for migrants and residents seems to strengthen the predictions of the AIV infection peak, the overall importance of this parameter (i.e. transmission rate (β)) reduces the informative power of the remaining
evaluated mechanisms, like the birth pulse ($B(t)$), the short-term immunity ($\sigma_s$) and the epidemiological state at which migrants enter a resident population ($M(t)$). However, those mechanisms might still be crucial. Indeed, the correlation matrix (Figure 4) shows that the immune rate ($\sigma$) and the transmission rate ($\beta$) could be parameters of importance and are highly correlated with parameters that significantly influence the autumn infection peak, like the ratio of migrants to residents ($Pr_{mig}$) and the amplitude of migratory replacement ($R_{amp}$). However, the correlation between such potentially important parameters also indicates that we require more information to narrow their potential range, otherwise the estimates become rather uninformative.

Birth pulses have previously been shown to be of importance in AIV infection dynamics in wild waterfowl (Hénaux et al. 2013), and appeared to be fundamental to produce annual infection peaks in empirically validated disease models (Hosseini, Dhondt & Dobson 2004; He 2005; Begon et al. 2009). Avril et al. (2016) showed that migratory juvenile mallards had a consistently higher risk of getting infected with AIV compared to adults. Hénaux et al. (2013) in particular showed that the early autumn AIV infection peak in a major host species across the North American continent, the blue-winged teal ($Anas discors$), was mainly due to infections in immunologically naive juveniles, and that only a small proportion of adults were within the susceptible pool and contributed to the transmission dynamics. Although knowledge on the number of migrants among adults was not included in that study, our results raise questions whether accounting for the underlying geography of the locations at which the birds were sampled, including associated differences in their migration strategies, could lead to other conclusions. Migration routes across the North American continent are grouped into four major north-south stretching flyways, and phylogenetic analysis of AIV indeed indicate that those flyways represent corridors for gene flow with more restricted
east-west gene flow, suggesting that migration of waterfowl occurs on a large scale from
north to south with little longitudinal mixing (Lam et al. 2012; Fourment, Darling & Holmes
2017, but see Krauss et al. 2010 for bottleneck in wader migration within North America).
The preferentially north-south migration across a broad east-west front may restrict the
origin and number of migrants within wetlands along the different migratory routes and
reduce their influence on the local AIV infection dynamics. In contrast, the wetlands in
central-northern Europe (e.g. the Netherlands) are within a bottleneck of the East-Atlantic
Flyway in which most routes of waterfowl from a vast geographical origin merge (Scott &
Pose 1996).

In our effort to construct relatively simple models allowing for comprehensive testing of a set
of hypothesised drivers for local AIV infection dynamics, we had to make a considerable
number of assumptions. Possibly the most important one is that we ignored the existence of
viral subtypes, and that AIV infection might elicit subtype specific immunity against further
infections (Latorre-Margalef et al. 2017). However, ducks may show limited immune
responses to AIV infection contrasting findings from e.g. chickens (Kida, Yanagawa &
Matsuoka 1980) and can quickly be re-infected with the same AIV subtype (Chaise et al.
2014) providing support for our simplifying approach to ignore potential antigenic variation
in AIV infected mallards. Furthermore, like most SIR(S) modelling approaches, we ignore
individual variation and the potentially important role of transmission heterogeneity and
“superspreaders” in the infection dynamics (e.g. Lloyd-Smith et al. 2005). However, although
we consider this of great importance, empirical data to support the existence of such
transmission heterogeneity for AIV among conspecifics within wildlife populations is thus far
lacking. Finally, the nature of the empirical data set that we used, e.g. one annual cycle at
one location for one bird population, might limit our ability to extrapolate our findings.
However, the temporal pattern and amplitude of the epizootic is comparable to what has been found in other studies in north-western Europe (e.g. Munster et al. 2007) and temperate areas in North America (e.g. Lisovski, Hoye & Klaassen 2017). Interestingly, despite some profound geographical variation in AIV infection patterns (Gaidet et al. 2012; Lisovski, Hoye & Klaassen 2017), globally the drivers for those patterns in AIV prevalence appear to be the same.

Management Implications

Avian influenza viruses are currently an increasing threat to the global poultry production sector and to public health (Hien, de Jong & Farrar 2004). The poultry industry and trade is an important part of this problem, with some highly pathogenic AIV strains being endemic in poultry in several countries in Africa and Asia, where also low pathogenic AIV is sometimes more readily circulating among domestic than wild birds (Hassan et al. 2017). Irrespectively, wild birds, and notably birds of the order Anseriformes (ducks and geese), are the ancestral reservoir host for AIV (Caron, Capelle & Gaidet 2017) and remain of key importance for global AIV diversity (Alexander 2007), notably in the face of readily reassorting high pathogenic AIV virus such as H5 clade 2.3.4.4 (Lee et al. 2017). Anseriformes also play a major role in the dispersal of AIV (Alexander 2007), including dispersal of highly pathogenic strains (e.g. Lycett et al. 2016); the latter most likely through spill-back from poultry (Messenger, Barnes & Gray 2014). It is for these reasons that an understanding of the ecology and transmission of AIV in wildlife, and migratory waterbirds in particular, is required to assist its management and control in livestock and humans in the future (Kuiken et al. 2005, Coker et al. 2011). Mathematical models allow probing the complex dynamics of host-pathogen interactions to help identify the mechanisms of transmission, enabling prediction and possibly prevention of
outbreaks. In spite of AIV infection dynamics being arguably one of the best studied avian-wildlife host-pathogen systems, our study highlights that we typically lack crucial information allowing identifying and quantifying the major mechanisms that lead to high prevalence levels in cases where migrants are involved; i.e., data on the number and turnover of migrants in a bird population. Thus, besides maintaining efforts in virus sampling and growing our understanding of virus diversity and evolution, their temporal occurrence and host range (Olsen et al. 2006; Munster et al. 2007; Caron, Capelle & Gaidet 2017) we additionally need increased efforts in recording of host demography. Given the here revealed importance of migration, and notably the timing and strategy of migration, it appears crucial to extend the wildlife disease surveillance database with demographic features such as the timing of birth and density, as well as turnover. Turnover can be estimated by flow models (Nolet & Drent 1998; Drever & Hrachowitz 2015), by combining counts with concurrent (re)sightings of marked individuals (e.g. Frederiksen et al. 2001) or by behavioural-based simulations of stopover site use (Nolet et al. 2016; Stillman et al. 2015). Knowledge of these parameters would allow us to use more in depth mathematical models allowing the estimation of e.g. transmission-, recovery- and immune rates, the key processes in host-pathogen interactions (McCallum 2000). Therefore, we believe that besides unravelling the mechanistic understanding of infection dynamics of wildlife diseases, understanding demographic patterns, especially for systems that involve considerable numbers of migratory individuals, are as important as pathogen detection.

Acknowledgements

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Authors’ contributions

MK, JvD, BN, DK, RF and SL conceived the research. SL analysed the data. SL and MK wrote the paper and all authors contributed significantly to the drafts and gave final approval for publication.

Data accessibility


References


support one-health research for policy on emerging zoonoses. Lancet Infectious Diseases 11, 326-331.


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Table 1: The parameters of the basic model and model modifications. If the value of a parameter is a single integer, the parameter was held fixed during the Markov Chain Monte Carlo (MCMC) simulation. All other parameters were optimised within the given range. Large numbers on the left group parameters that are unique to a certain model modification. See methods for references and validation of the defined parameter ranges.

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<th>Symbol</th>
<th>Definition</th>
<th>Value/Range</th>
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<td>transmission rate</td>
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<td>bird$^{-1}$ day$^{-1}$</td>
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<td>$\gamma$</td>
<td>recovery rate</td>
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<tr>
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<td>immune rate</td>
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<td>mortality rate</td>
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</tr>
<tr>
<td>$N_{\text{pulse}}$</td>
<td>number of hatchlings per pair</td>
<td>$4$</td>
<td>individuals</td>
</tr>
<tr>
<td>$m_{\text{juv}}$</td>
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<td>bird$^{-1}$ day$^{-1}$</td>
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<td>$R_{\text{amp}}$</td>
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<td>days</td>
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<td>kurtosis of migratory replacement</td>
<td>$2$ to $3$</td>
<td>days</td>
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Figure legends

Figure 1: The structure of the basic model and the main differences of the modifications that are based on five potential mechanisms that may drive local AIV infection dynamics in wild birds. For the basic model, the grey box shows the flowchart of the movement of migrant (M) and resident (R) individuals between the susceptible (S), infectious (I) and recovered (R) compartments as described by the model equations 1-6. Natural mortality (m) is not depicted, but is assumed to occur within all three compartments and at the same rate for all individuals (i.e. resident and migrant). The graph below the grey box shows the general annual demographic dynamics of resident mallards (dashed line) and migratory mallards (solid line) visiting the study site during the annual cycle. For the 1st model modification, the bold dashed line shows the potential dynamics of the resident population with a more pronounced birth pulse B(t). The 2nd model modification assumes a reduced immune rate (σ) and thus a faster loss of immunity against AIV infections. In the 3rd model modification, relatively more migrants enter into the pool of susceptible (S) individuals. In the 4th model modification, the transmission rate (β) is modelled separately and has different values for migrants (β_M) and residents (β_R). For the 5th model modification, the R(t) curve describes the amount and the shape at which migrants within the infectious (I) and the recovered (R) pool are replaced by new susceptible migrants.

Figure 2: Ranked model scenarios based on median WAIC (‘model cost’) of the model fit. White bars indicate scenarios with a single modification on top of the basic model. The black bar shows the basic model without any modification. Models with lower WAIC represent better model fits. The bars represent the median WAIC over 25 independent MCMC chains with random selection of initial priors within the range of the respective parameter. Error bars indicate 95% confidence intervals. The inclusion of the five model modifications to the basic model are shown below the bar plot, with a
cross indicating that the particular modification was included in the scenario. The model scenarios are
1) Birth Pulse, 2) Short-term immunity, 3) Increase of Susceptible Migrants, 4) Differential Susceptibility and 5) Replacement of Migrants. Below, all estimated parameter values across the 32 scenarios are shown with the 50% (circle) and the 10% and 90% percentiles of the posterior distributions (10,000 iterations). The grey areas between the dashed lines indicate the pre-set parameter ranges. In case of the transmission rate (β) and immune rate (σ), the dotted lines indicate the reduced boundaries of the parameter for the 4th differential susceptibility and the 2nd short-term immunity modifications.

Figure 3: Results of three model scenarios: the best-ranked scenario (with 3rd, 4th and 5th modification, Rank 1), the scenario with the most influential modification only (5th modification, Rank 12), and the scenario with the second most influential modification only (4th modification; Rank 22). The left column shows which of the model modifications were included in the respective scenario. The middle column shows the observed AIV prevalence levels (±95% CI) at the study site (dashed line with diamond symbols), and the model prediction (bold line) of the best fitting model with the respective modifications. Grey area around model predictions indicate the sensitivity range of the fit (e.g. ±95% CI). The underlying demography for each depicted scenario is shown in the right column with absolute numbers of individuals (black line) consisting of migrants (dotted line) and residents (dashed line). The replaced migrants (R(t)) is also shown as the absolute number of individuals replaced at time t (in days). Additionally, the rate of change in individuals (∆ Individuals) is shown for residents indicating birth (light grey bars) and migrants indicating initial arrival (dark grey bars).

Figure 4: The parameters of the best ranked model scenario (matrix diagonal) and the correlation matrix of all parameters from the last 2,500 MCMC iterations. The intensity of grey and shape of the
ellipsoids represent the strength (dark colour and narrow ellipse represent correlation coefficients close to 1 or -1) and direction of the correlation.
Basic Model

1. Birth Pulse

2. Short-term Immunity

3. Increase of susceptible Migrants

4. Differential Susceptibility

5. Replacement of Migrants

# Individuals

time (1 annual cycle)
<table>
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<td>$\beta_M$</td>
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<tr>
<td>$\gamma$</td>
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<tr>
<td>$\sigma$</td>
<td>0.044</td>
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<td>$B_{\text{sd}}$</td>
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<td>$P_{\text{mig}}$</td>
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<td>2.005</td>
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</tbody>
</table>
Supplementary Materials for

The differential role of migrants and residents in local avian influenza infection dynamics

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S1: Model equations

S2: Model fitting results and correlation matrices
S1: Model equations

The ordinary differential equation for the background model (eq. 1-6) are shown in the main text. Here, the structural changes that occurred due to one of the five model modifications will be shown.

1. Birth pulse

Resident adult population:

\[
\frac{dS_R(t)}{dt} = -\beta (I_R + I_M)S_R + \sigma R_R - \eta S_R - m_S R_R
\]

\[
\frac{dI_R(t)}{dt} = \beta (I_R + I_M)S_R - \gamma I_R + \eta I_R - m_I R_R
\]

\[
\frac{dR_R(t)}{dt} = \gamma I_R - \sigma R_R - m_R R_R
\]

Resident juvenile population:

\[
\frac{dS_R(t)}{dt} = -\beta (I_R + I_M)S_R + \sigma R_R - \eta S_R - m_j S_R + B (0.5 \cdot N_{pop})N_{pulse}
\]

\[
\frac{dI_R(t)}{dt} = \beta (I_R + I_M)S_R - \gamma I_R + \eta I_R - m_j I_R
\]

\[
\frac{dR_R(t)}{dt} = \gamma I_R - \sigma R_R - m_j R_R
\]

Migrant population:

As eq. 4-6
3. Increase of susceptible migrants

*Resident population:*

As eq. 1-3

*Migrant population:*

\[
\frac{dS_M(t)}{dt} = -\beta (I_R + I_M)S_M + \sigma R_M - \eta S_M - mS_M \\
+ M \left( \left( \frac{S_R}{S_R + I_R + R_R} \right) + \left( \frac{S_R}{S_R + I_R + R_R} \right) b \right) N_{pop} Pr_m
\]

\[
\frac{dI_M(t)}{dt} = \beta (I_R + I_M)S_M - \gamma I_M + \eta I_M - mI_M + M \left( \frac{S_R}{S_R + I_R + R_R} \right) N_{pop} Pr_m
\]

\[
\frac{dR_M(t)}{dt} = \gamma I_M - \sigma R_M - mR_M + M \left( \left( \frac{S_R}{S_R + I_R + R_R} \right) - \left( \frac{S_R}{S_R + I_R + R_R} \right) b \right) N_{pop} Pr_m
\]

4. Differential susceptibility

*Resident population:*

\[
\frac{dS_R(t)}{dt} = -\beta_R - (I_R + I_M)S_R + \sigma R_R - \eta S_R - mS_R + B(0.5 \cdot N_{pop}) N_{hatch}
\]

\[
\frac{dI_R(t)}{dt} = \beta_R (I_R + I_M)S_R - \gamma I_R + \eta I_R - mI_R
\]

\[
\frac{dR_R(t)}{dt} = \gamma I_R - \sigma R_R - mR_R
\]

*Migrants:*

\[
\frac{dS_M(t)}{dt} = -\beta_M (I_R + I_M)S_M + \sigma R_M - \eta S_M - mS_M + M \left( \frac{S_R}{S_R + I_R + R_R} \right) N_{pop} Pr_m
\]

\[
\frac{dI_M(t)}{dt} = \beta_M (I_R + I_M)S_M - \gamma I_M + \eta I_M - mI_M + M \left( \frac{I_R}{S_R + I_R + R_R} \right) N_{pop} Pr_m
\]

\[
\frac{dR_M(t)}{dt} = \gamma I_M - \sigma R_M - mR_M + M \left( \frac{R_R}{S_R + I_R + R_R} \right) N_{pop} Pr_m
\]
4. Replacement of migrants

Resident population:

As eq. 1:3

Migrants:

\[
\frac{dS_M(t)}{dt} = -\beta_M(I_R + I_M)S_M + \sigma M - \eta S_M - m S_M + M \left( \frac{S_R}{S_R + I_R + R_R} \right) N_{pop} Pr_m + R(I_m + R_M)
\]

\[
\frac{dI_M(t)}{dt} = \beta_M(I_R + I_M)S_M - \gamma I_M + \eta I_M - m I_M + M \left( \frac{I_R}{S_R + I_R + R_R} \right) N_{pop} Pr_m - R(I_m)
\]

\[
\frac{dR_M(t)}{dt} = \gamma I_M - \sigma R_M - m R_M + M \left( \frac{R_R}{S_R + I_R + R_R} \right) N_{pop} Pr_m - R(R_m)
\]
S2. Model fitting results and correlation matrices

This supplemental information shows the model fitting results (minimum and percentiles) and the correlation matrices from the sensitivity analysis of the first 17 best-ranked scenarios.

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